3.1

1. Is x - 5 a factor of each trinomial? Justify your answer.

a)
$$3x^2 + 3x - 60$$

Write the trinomial as:
 $(x - 5)(3x + b)$
 $= 3x^2 + (b - 15)x - 5b$
Equate constant terms.
 $-5b = -60$, so $b = 12$
Check:
 $(x - 5)(3x + 12)$
 $= 3x^2 - 3x - 60$
So, $x - 5$ is not a factor.
b) $3x^2 - 13x - 10$
Write the trinomial as:
 $(x - 5)(3x + b)$
 $= 3x^2 + (b - 15)x - 5b$
Equate constant terms.
 $-5b = -10$, so $b = 2$
Check:
 $(x - 5)(3x + 12)$
 $= 3x^2 - 3x - 60$
So, $x - 5$ is not a factor.
b) $3x^2 - 13x - 10$
Write the trinomial as:
 $(x - 5)(3x + b)$
 $= 3x^2 + (b - 15)x - 5b$
Equate constant terms.
 $-5b = -10$, so $b = 2$
Check:
 $(x - 5)(3x + 2)$
 $= 3x^2 - 13x - 10$
So, $x - 5$ is a factor.

2. Factor.

a)
$$0.5x^2 - 0.4x - 1.2$$
b) $3(x - 3)^2 + 2(x - 3) - 5$ $= 0.1(5x^2 - 4x - 12)$ Guess and test factors ofGuess and test factors of3 with factors of -5. $= 0.1(x - 2)(5x + 6)$ $= (3x - 4)(x - 4)$

3. Factor.

a)
$$81x^2 - 4y^2$$

= $(9x)^2 - (2y)^2$
= $(9x + 2y)(9x - 2y)$

b)
$$49(x - 4)^2 - 9(5y - 2)^2$$

= $[7(x - 4)]^2 - [3(5y - 2)]^2$
= $[7(x - 4) + 3(5y - 2)][7(x - 4) - 3(5y - 2)]$
= $(7x + 15y - 34)(7x - 15y - 22)$

3.2

4. Solve by factoring. Verify the solutions.

a) $20x^2 + 3x - 2 = 0$ (4x - 1)(5x + 2) = 0Either 4x - 1 = 0; then x = 0.25; or 5x + 2 = 0, then x = -0.4b) $6x^2 - 21x + 18 = 0$ $3(2x^2 - 7x + 6) = 0$ 3(2x - 3)(x - 2) = 0Either 2x - 3 = 0, then x = 1.5; or x - 2 = 0, then x = 2 c) (x - 5)(x + 8) = 14 $x^2 + 3x - 54 = 0$ (x - 6)(x + 9) = 0Either x - 6 = 0, then x = 6; or x + 9 = 0, then x = -9I used mental math to verify the solutions. d) $6x^2 = 8x$ 2x(3x - 4) = 0Either 2x = 0, then x = 0; or 3x - 4 = 0, then $x = \frac{4}{3}$

5. Two numbers have a sum of 20 and a product of 84. Use a quadratic equation to determine the numbers.

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Let one number be x. Then the other number is 20 - x.

An equation is: x(20 - x) = 84

20x - x^2 - 84 = 0

x^2 - 20x + 84 = 0

(x - 14)(x - 6) = 0

x = 14 or x = 6

The numbers are 14 and 6.
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3.3

6. Solve each equation.

a) $(2x + 1)^2 + 4 = 49$	b) $-3 + (3 - 2x)^2 = 5$
$(2x + 1)^2 = 45$	$(3 - 2x)^2 = 8$
$2x + 1 = \pm \sqrt{45}$	$3-2x=\pm\sqrt{8}$
$2x = -1 \pm \sqrt{45}$	$2x = 3 \pm \sqrt{8}$
$x=\frac{-1\pm\sqrt{45}}{2}$	$x=\frac{3\pm\sqrt{8}}{2}$

7. Solve each equation by completing the square.

a)
$$x^{2} + 4x + 2 = 0$$

 $x^{2} + 4x = -2$
 $x^{2} + 4x + 4 = -2 + 4$
 $(x + 2)^{2} = 2$
 $x + 2 = \pm \sqrt{2}$
 $x = -2 \pm \sqrt{2}$
 $x = \frac{1}{3} + \frac{1}{9} + \frac{1}{9} = \frac{1}{3} + \frac{1}{9} + \frac{1}{$

3.4

8. Solve each quadratic equation.

a)
$$2x^{2} - 6x + 1 = 0$$

Substitute:
 $a = 2, b = -6, c = 1$
 $in: x = \frac{-b \pm \sqrt{b^{2} - 4ac}}{2a}$
 $x = \frac{6 \pm \sqrt{(-6)^{2} - 4(2)(1)}}{2(2)}$
 $x = \frac{6 \pm \sqrt{28}}{4}$
 $x = \frac{6 \pm 2\sqrt{7}}{4}$
 $x = \frac{3 \pm \sqrt{7}}{2}$
b) $(x + 1)(x + 2) = x$
 $x^{2} + 2x + 2 = 0$
Substitute: $a = 1, b = 2, c = 2$
 $in: x = \frac{-b \pm \sqrt{b^{2} - 4ac}}{2a}$
 $x = \frac{-2 \pm \sqrt{2^{2} - 4(1)(2)}}{2(1)}$
 $x = \frac{-2 \pm \sqrt{-4}}{2}$
There are no real roots.

9. A truck was travelling at 23 m/s. It decelerated for 15 s. The distance travelled by the truck, d metres, during this time is given by the formula $d = 23t - 0.6t^2$, where *t* is the time in seconds. How long did it take the truck to travel 60 m? Give the answer to the nearest tenth of a second.

In $d = 23t - 0.6t^2$, substitute: d = 60, then solve for t. $60 = 23t - 0.6t^2$ $0.6t^2 - 23t + 60 = 0$ Substitute: a = 0.6, b = -23, c = 60 in: $t = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$ $t = \frac{23 \pm \sqrt{(-23)^2 - 4(0.6)(60)}}{2(0.6)}$ $t = \frac{23 \pm \sqrt{385}}{1.2}$ Either $t = \frac{23 + \sqrt{385}}{1.2}$, so t = 35.5Or $t = \frac{23 - \sqrt{385}}{1.2}$, so t = 2.8Since the truck decelerated for only 15 s, t = 35.5 s is not a solution.

So, the truck took approximately 2.8 s to travel 60 m.

3.5

10. Without solving, determine whether each equation has one, two, or no real roots.

a) $2x^2 - 1.8x - 1.25 = 0$ b) $-2x^2 + 3x - 10 = 0$ In $b^2 - 4ac$, substitute: a = 2, b = -1.8, c = -1.25 a = -2, b = 3, c = -10 $b^2 - 4ac = (-1.8)^2 - 4(2)(-1.25)$ $b^2 - 4ac = 3^2 - 4(-2)(-10)$ = 13.24 = -71Since $b^2 - 4ac > 0$, the equation has 2 real roots. Since $b^2 - 4ac < 0$, the equation has no real roots.

- **11.** Consider the equation $8x^2 5x + k = 0$. Determine the values of k in each case:
 - a) The equation has no real roots.

 $8x^{2} - 5x + k = 0$ In $b^{2} - 4ac$, substitute: a = 8, b = -5, c = k $b^{2} - 4ac = (-5)^{2} - 4(8)(k)$ = 25 - 32kFor no real roots, 25 - 32k < 0 $k > \frac{25}{32}$

b) The equation has exactly one real root.

Use the value of $b^2 - 4ac$ from part a. For exactly 1 real root, 25 - 32k = 0 $k = \frac{25}{32}$

c) The equation has two real roots.

Use the value of $b^2 - 4ac$ from part a. For 2 real roots, 25 - 32k > 0 $k < \frac{25}{32}$